

# Passive and Active Actuation of Droplet Motion

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# Overview

1. Superhydrophobicity

2. Gradients in Superhydrophobicity

3. Electrowetting

4. Moving Liquid Marbles

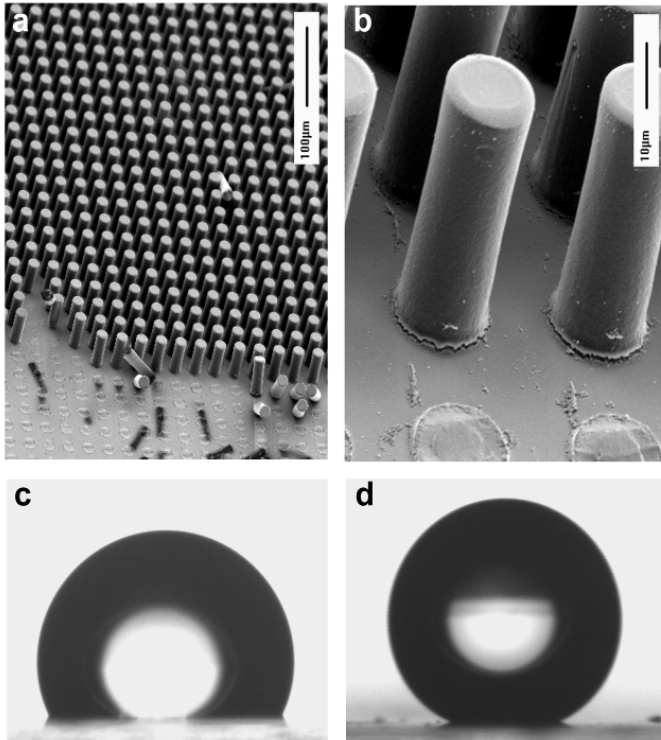
} Passive

} Active

# Superhydrophobicity

# Surface Structure

## Effect on Water

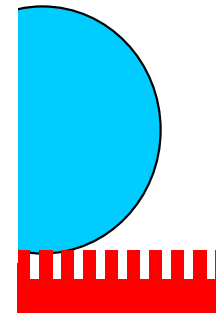


- a), b) Pillars  $D=15 \mu\text{m}$ ,  $L = 2D$
- c) Flat and hydrophobic
- d) Tall and hydrophobic

## “Skating” Droplets

Composite air-solid surface  
(Cassie-Baxter)

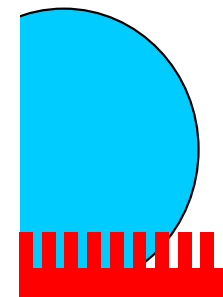
Low hysteresis: “Slippy” surface



## “Penetrating” Droplets

Based on roughness (Wenzel)

Large hysteresis: “Sticky” surface

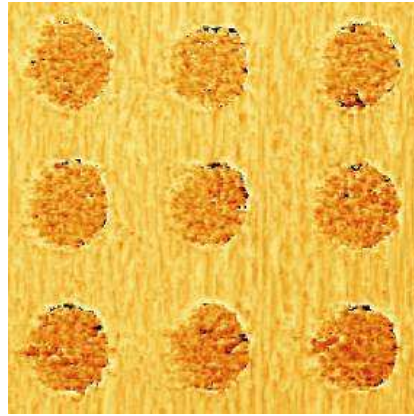


# Electrodeposited Surfaces

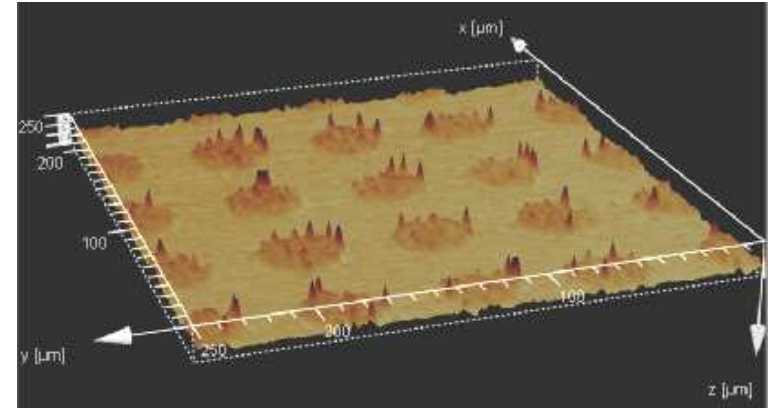
Diffusion limited aggregation –copper acid bath, fractal roughness



*Base Cu electroplated surface*

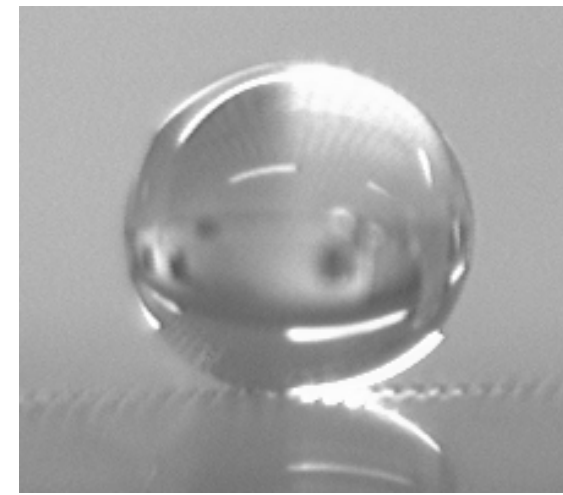
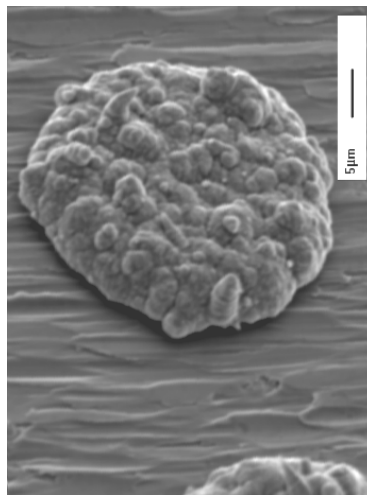
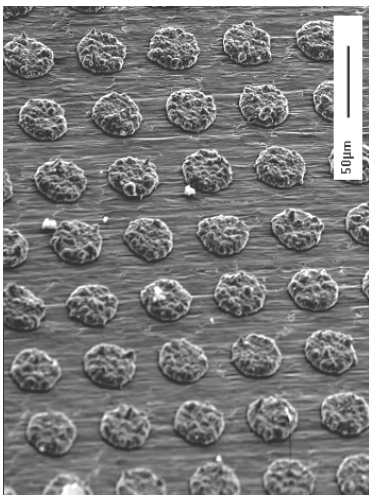


*Confocal image of a 30 $\mu$ m textured electroplated Cu*



*3D view of a electroplated copper sample*

“Chocolate Chip Cookies” - Electroplating through a mask



# Gradients in Superhydrophobicity

# Driving Force

## Local Cassie-Baxter Contact Angle

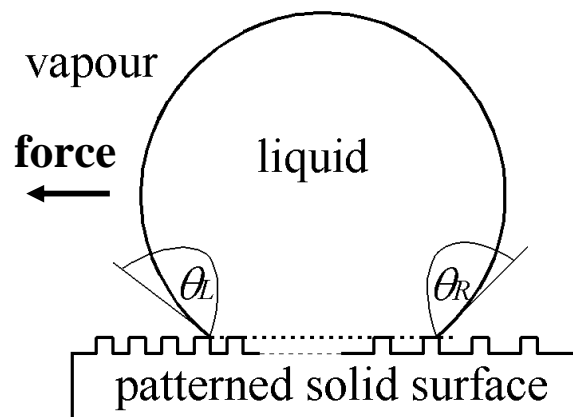
Make contact angle depend on position and surface chemistry  $\theta(x, \theta_e^s)$

Same surface chemistry, but vary Cassie-Baxter fraction across surface

$$\cos \theta_{CB}(x) = f(x) \cos \theta_e^s - (1-f(x))$$

## Driving Force

Droplet experiences different contact angles  $\Rightarrow$  driving force



$$\begin{aligned} \text{Force} &\propto \gamma_{LV}(\cos \theta_R - \cos \theta_L) \\ &\propto \gamma_{LV}(f_R - f_L)(\cos \theta_e^s + 1) \end{aligned}$$

*Need to overcome contact angle hysteresis*

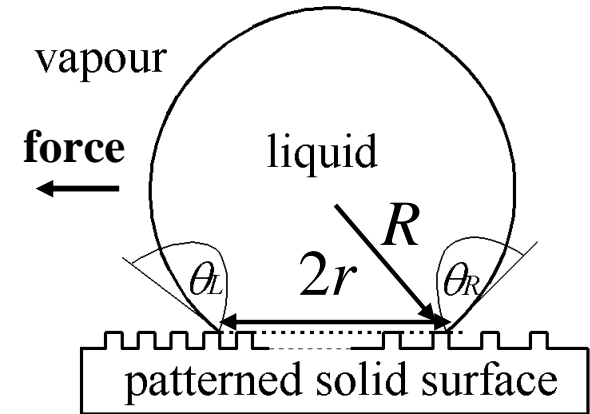
# Conditions for Motion

## Spherical Cap

Assume small contact area:

$$2r \approx 2R [2f_{\text{ave}}(x)(1 + \cos \theta_e^s)]^{1/2}$$

$$\begin{aligned} \text{Force/length} &= \gamma_{LV}(f_R - f_L)(\cos \theta_e^s + 1) \\ &= 2R \gamma_{LV} [2f_{\text{ave}}(x)]^{1/2} (1 + \cos \theta_e^s)^{3/2} (df/dx) \end{aligned}$$



## Defect Based Hysteresis Force

$$\text{Force/length} = \gamma_{LV} \Delta(\cos \theta) \approx \gamma_{LV} f(x) \log f(x)$$

## Drive Condition

$$(df/dx) > \text{constant} \times f_{\text{ave}}(x)^{1/2} \log f_{\text{ave}}(x) / [R(1 + \cos \theta_e^s)^{3/2}]$$

More  
superhydrophobic

Larger  
droplets



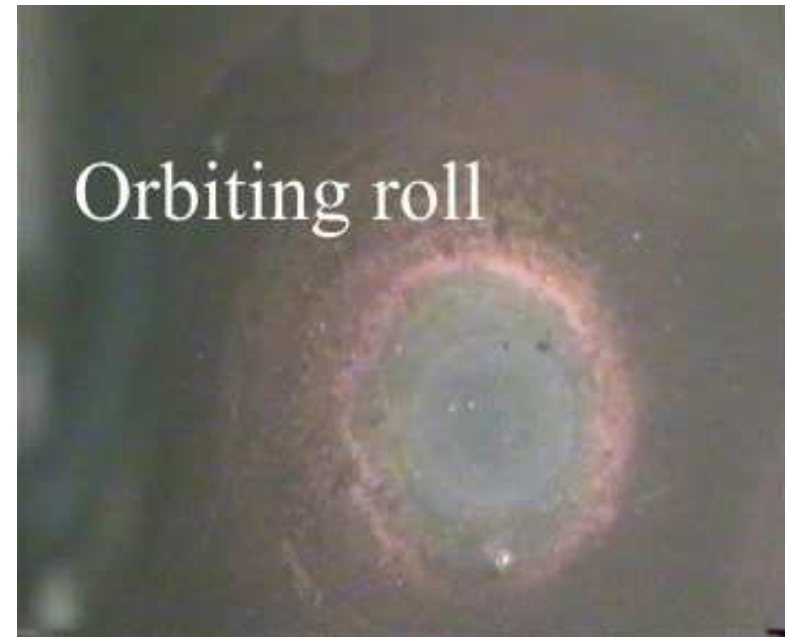
# Self-Actuated Motion

## Radial Gradient in Contact Angle

Electrodeposited copper – Diffusion limited aggregation

Fractal-like to overcome contact angle hysteresis

Radial gradient  $\theta(r)=110^\circ \rightarrow 160^\circ$



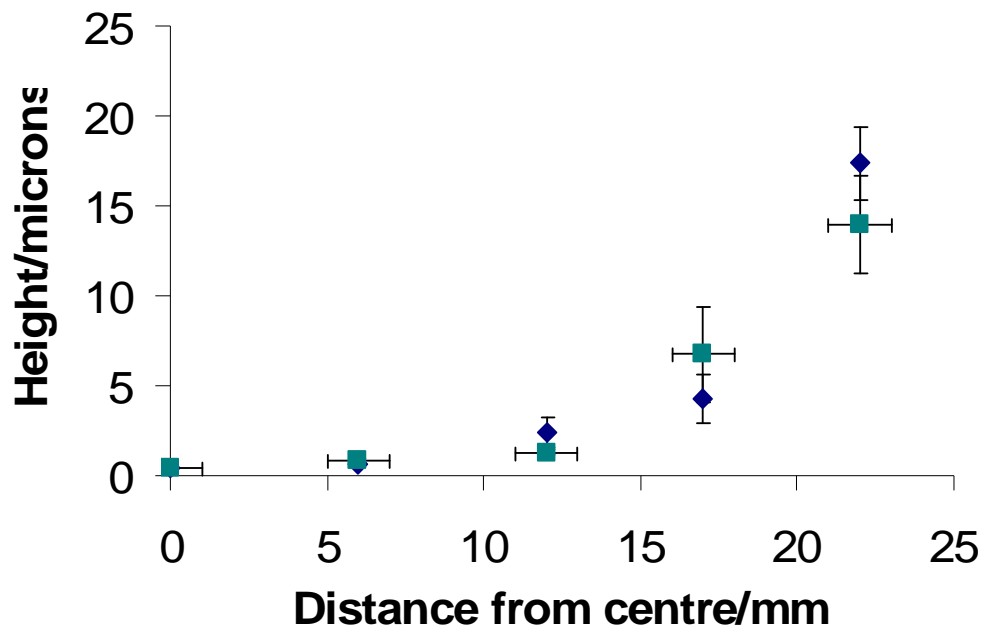
# Surface Profile

## Mechanism for Motion

Small slope on extremely low hysteresis surface?

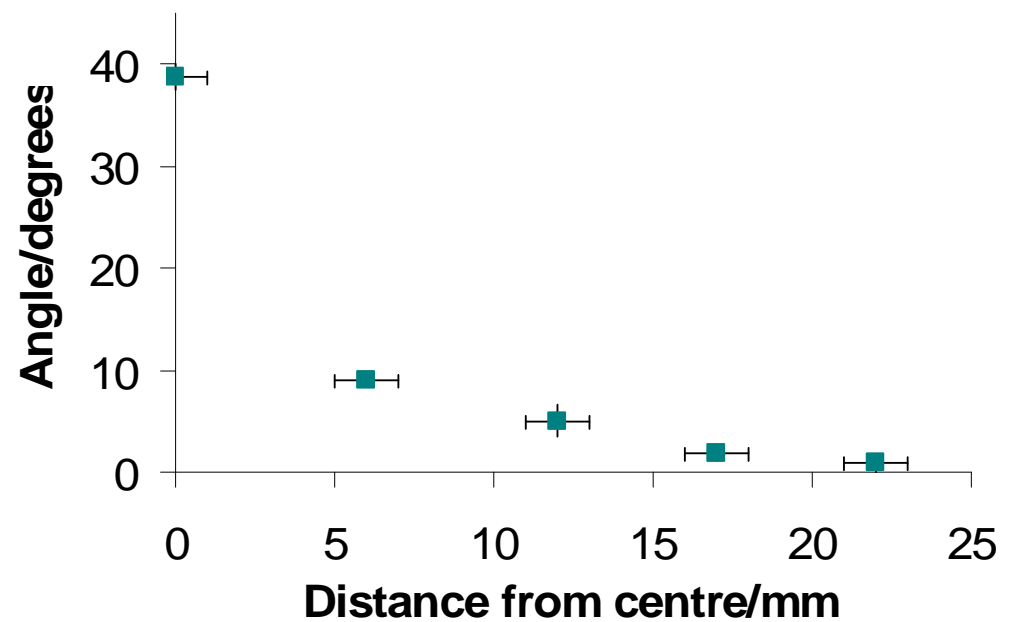
Truly contact angle driven?

### Surface Profile



Multiple profiles have been taken along different radial lines

### “Hysteresis”



Using radial view and tilt table tangential to radius

# Electrowetting on a Superhydrophobic Surface

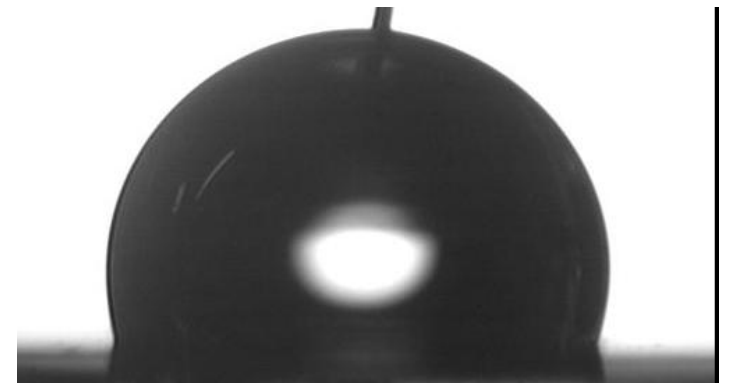
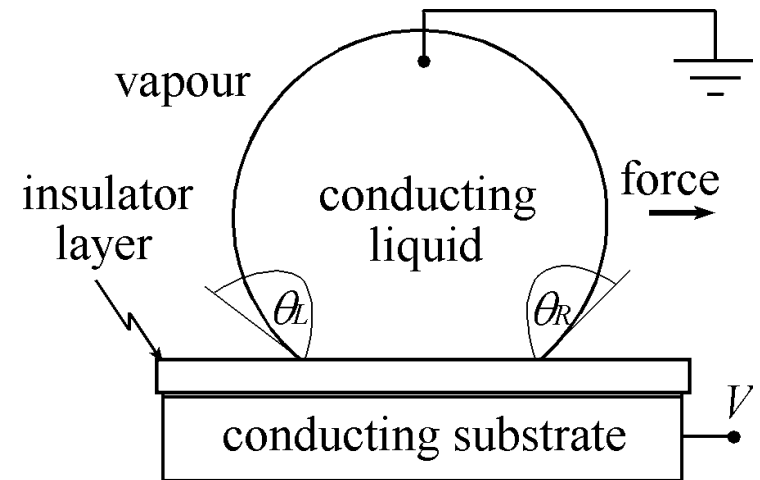
# Electrowetting-on-Dielectric (EWOD)

## Electrowetting Principle

- Conducting liquid on electrical insulator on conducting substrate
- Applying voltage electrically charges solid-liquid interface (i.e. a Capacitive effect)
- Droplet spreads and contact angle reduces

$$\cos \theta_e(V) = \cos \theta_e(0) + CV^2/2\gamma_{LV}$$

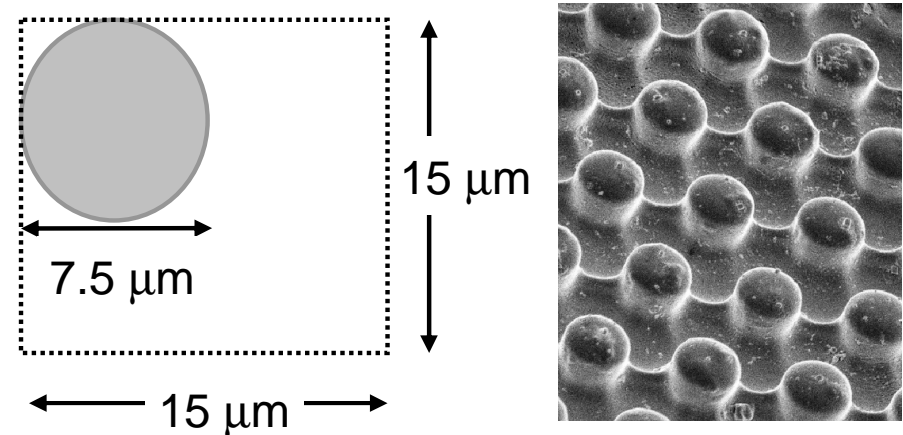
- Difference in angles at edge of droplet reflects an actuating force



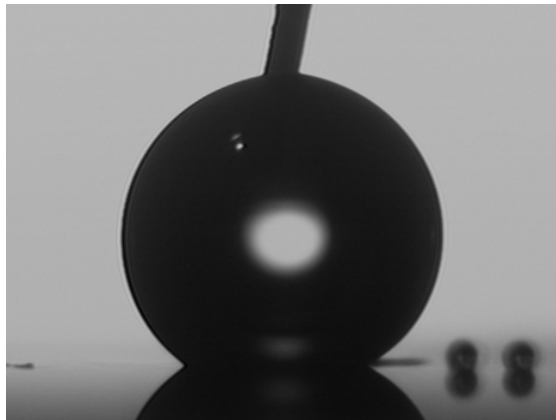
# Irreversible Electrowetting on S/H Surface

## Lithographic System

- Ti/Au on glass, SU-8 microposts, Teflon AF1600 capped
- Droplets of deionised water with 0.01M KCl and AC or DC



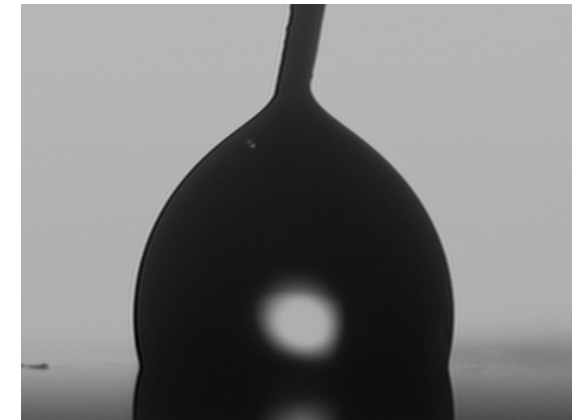
### Initial Shape



### Applied Voltage



### Voltage Removed



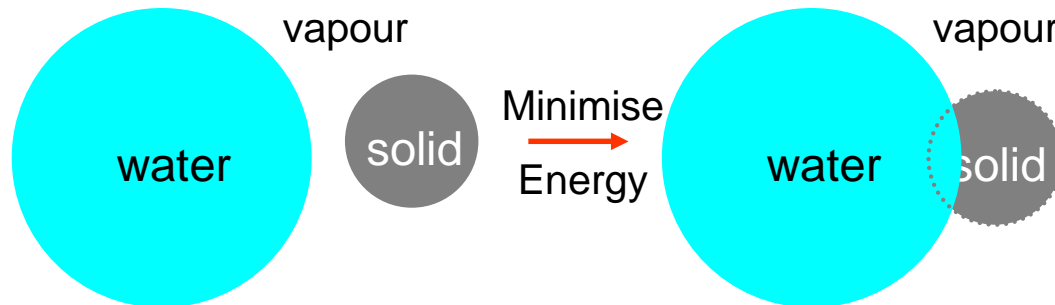
152°  114°

*Irreversible and so difficult for actuating motion*

# Liquid Marbles

# Liquid Marbles

- Hydrophobic Grains Adhere to the Water-Air Interface



$$\Delta F = -\pi R_g^2 \gamma_{LV} (1 + \cos \theta_e)^2$$

Lycopodium

Mobility



Lycopodium grains are 15-19  $\mu\text{m}$ , but monolayers can be achieved



Perfect non-wetting system with zero hysteresis  
Gravity flattens shape as volume increases

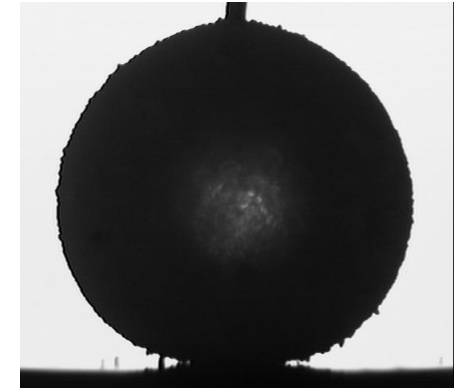
# Active Actuation of Marble Motion



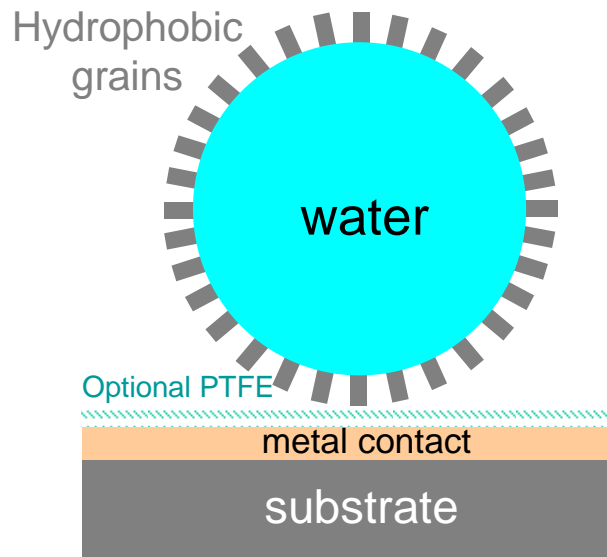
# “Electrowetting” of Liquid Marbles

- **Reversibility Idea**

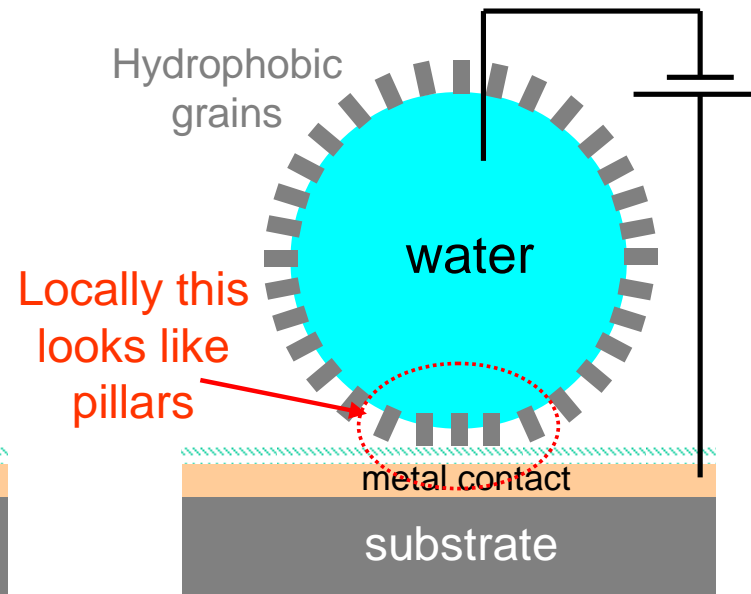
- Make the solid “pillars” adhere more to the liquid than to the substrate
- Provides insulating “pillars” **conformal** to the liquid shape
- More hydrophobic grains “stick out” further (i.e. taller pillars)



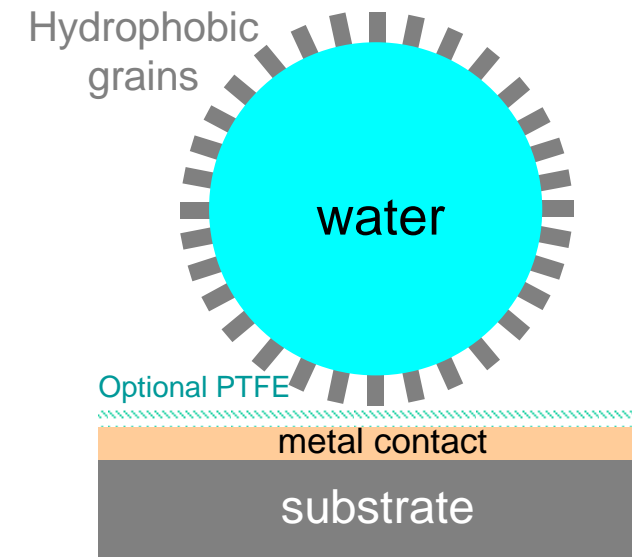
## Initial Shape



## Apply Voltage



## Remove Voltage



# Model for Liquid Marbles

Minimise total energy of a spherical cap

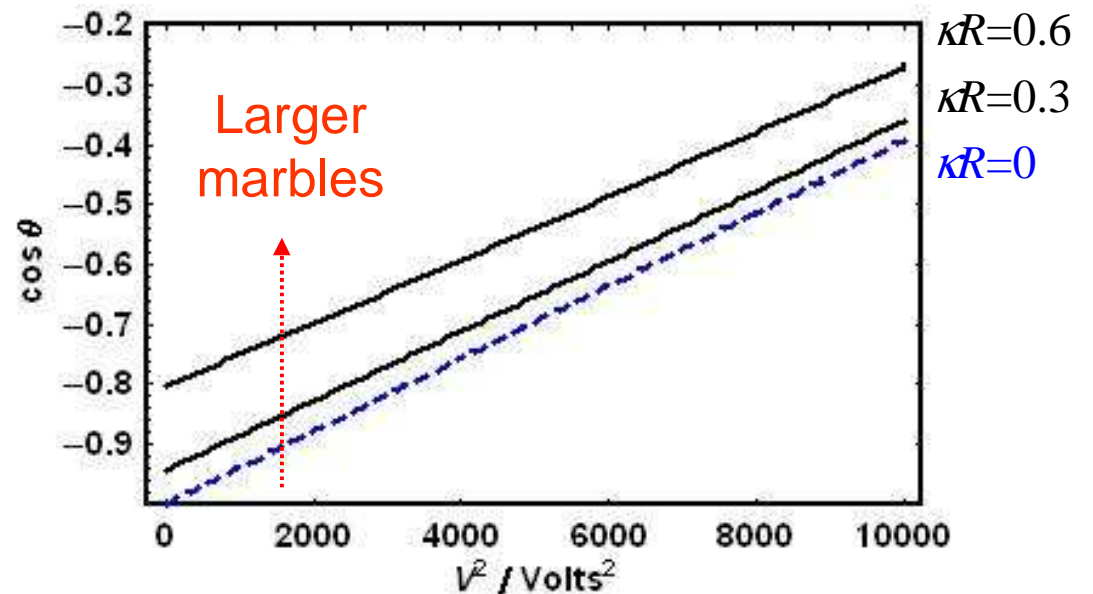
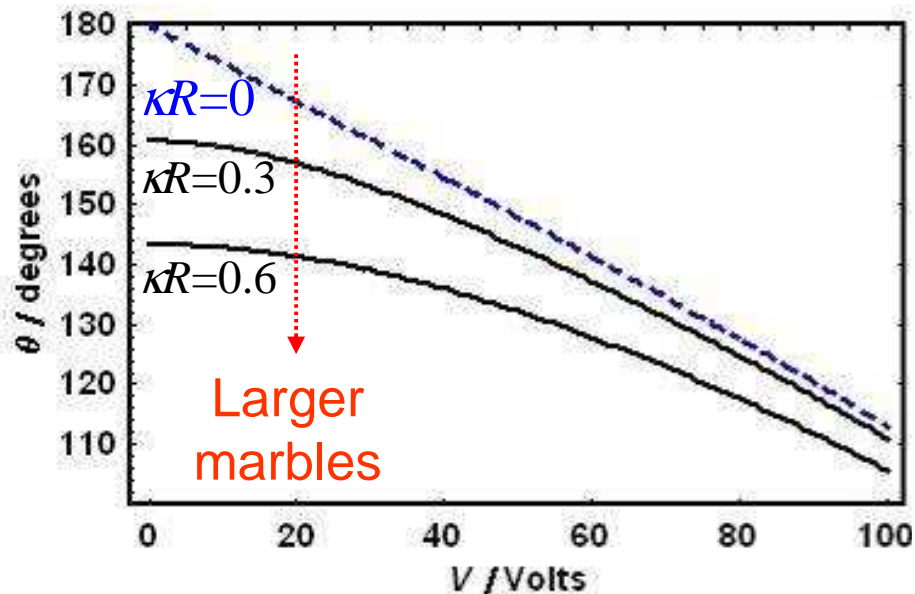
$$\cos \theta = \cos \theta_e + (\kappa h)^2/6 + CV^2/2\gamma_{LV}$$

From surface energy  
-1 for marble

Gravitational energy gives a drop  
size factor with  $h = h(\theta)$ , so non-linear

Capacitive energy  
from electrowetting

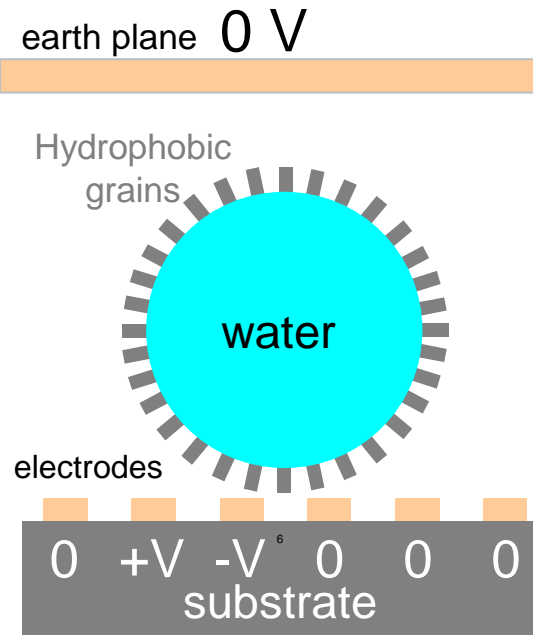
## Numerical Results



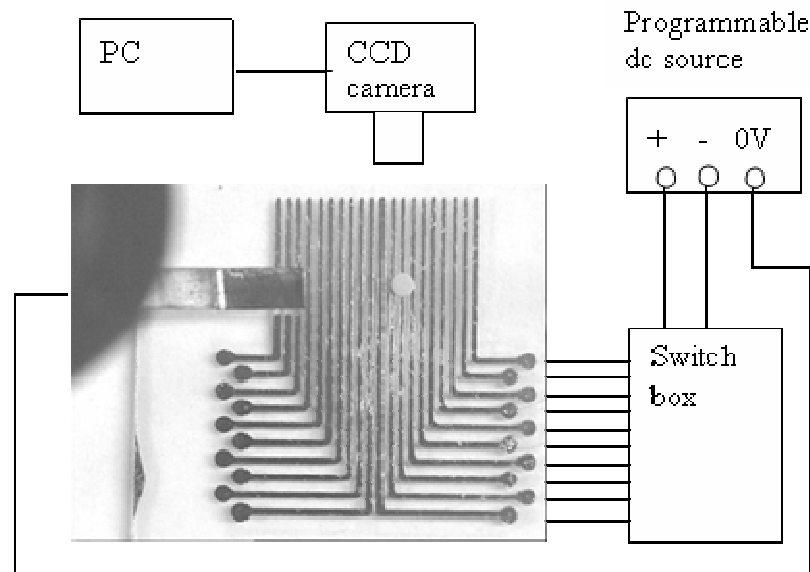
# A Hint of Controllable Motion

1. Liquid marble using hydrophobic lycopodium
2. Upper earth plane, planar strip electrodes, pairs switched to  $\pm 150$  V DC

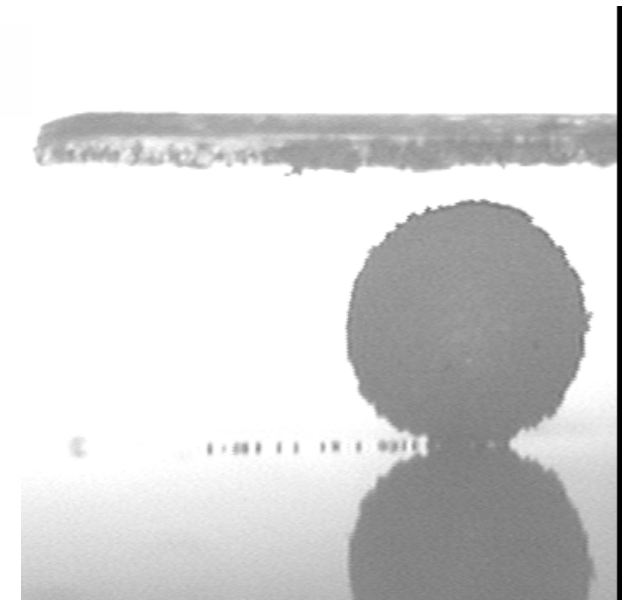
## Concept



## Method



## Results



# Summary

## 1. Passively Actuated Motion of Droplets

Appears possible via gradients in  $\theta_{CB}$

Outstanding questions about droplet threshold sizes

## 2. Voltage Actuated Motion

Problems remain on superhydrophobic surfaces

Can be achieved with liquid marbles

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# The End

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### Acknowledgements

EPSRC GR/R02184/01 and GR/S34168/01 –Dstl via

EPSRC/MOD JGS

EU COST Action D19 & P21

NOTTINGHAM  
TRENT UNIVERSITY

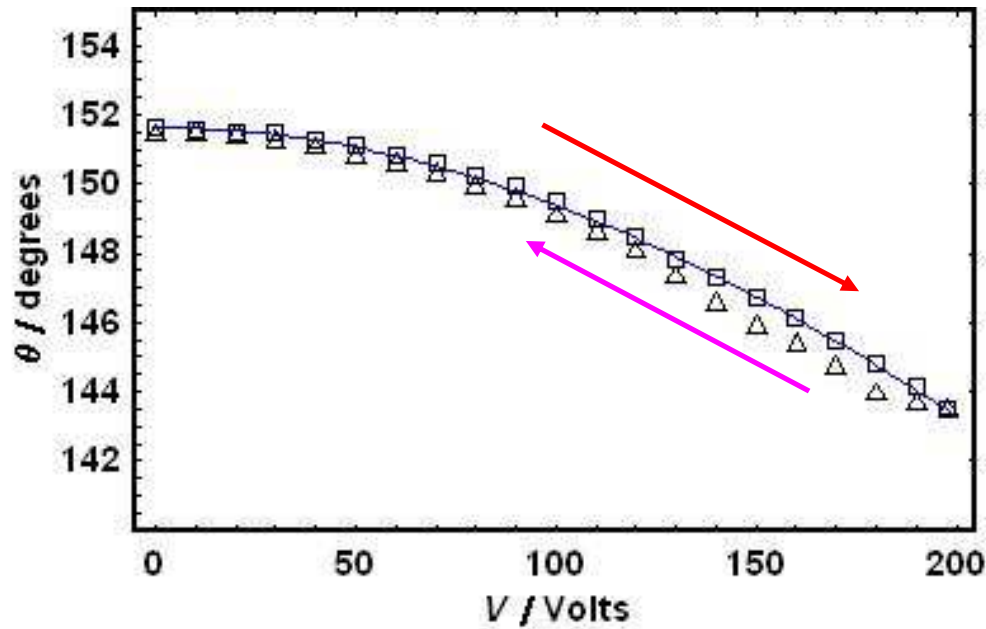
EPSRC

Engineering and Physical Sciences  
Research Council

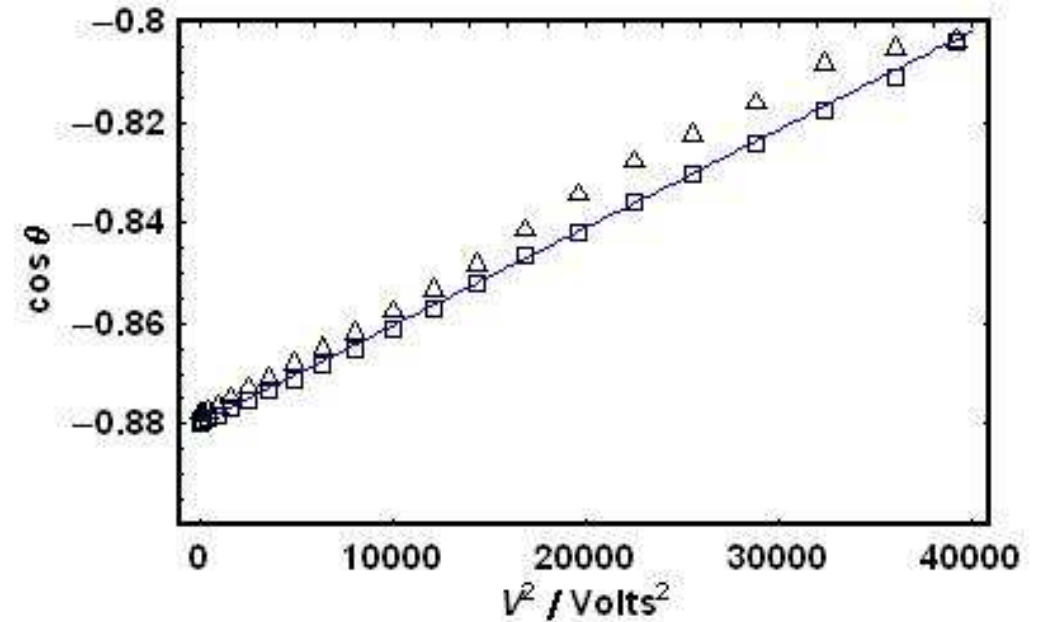


# 5. Results using Hydrophobic Silica

## Contact Angle

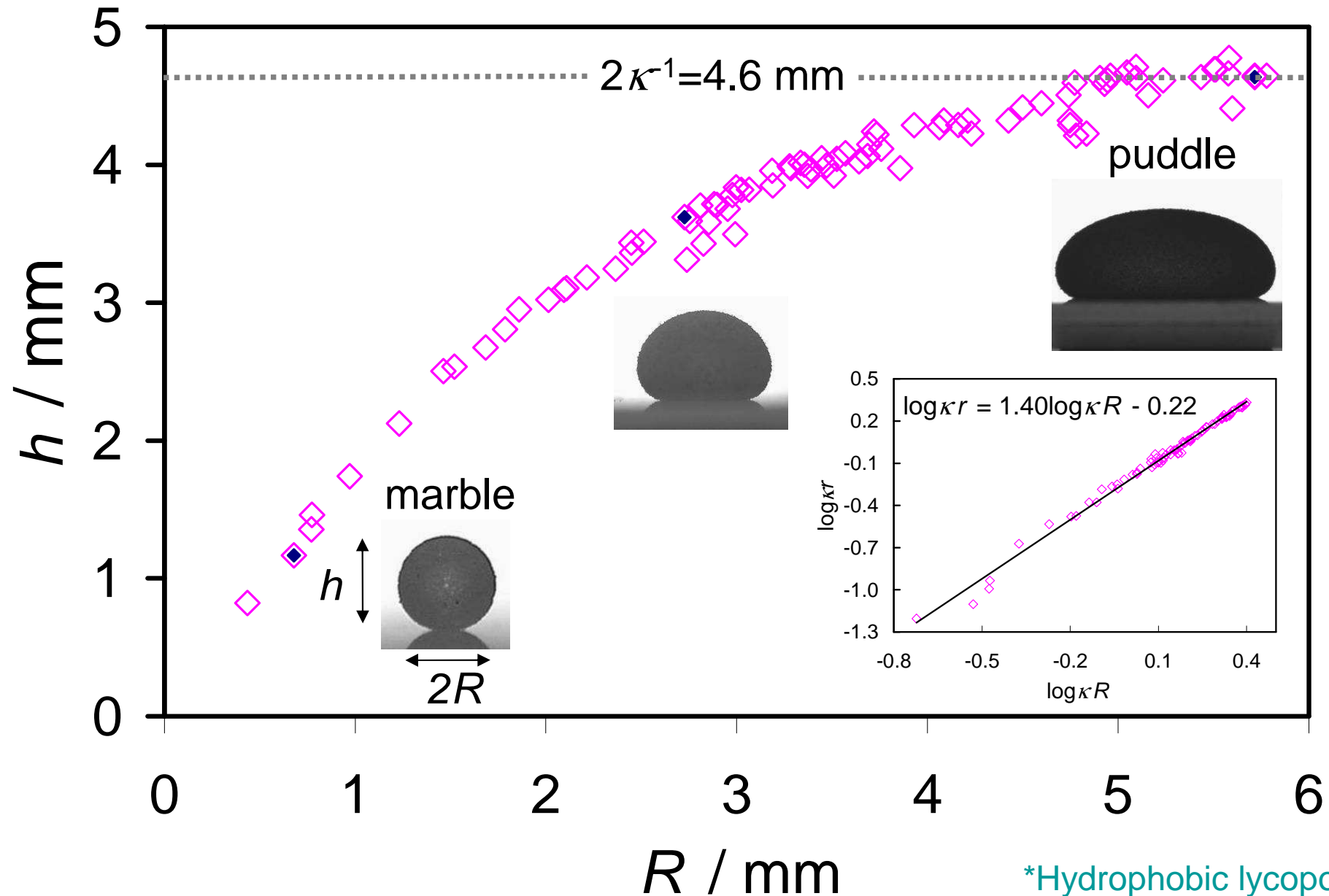


## Fitting



1. *No threshold* voltage
2. Virtually *no* contact angle *hysteresis*
3. Experiments show a limited range (155° to 130°)
4. Fit uses  $\kappa R=0.45$

# Perfect Non-Wetting Marbles\*



\*Hydrophobic lycopodium

# Electroplated Copper Surfaces

- Copper acid bath

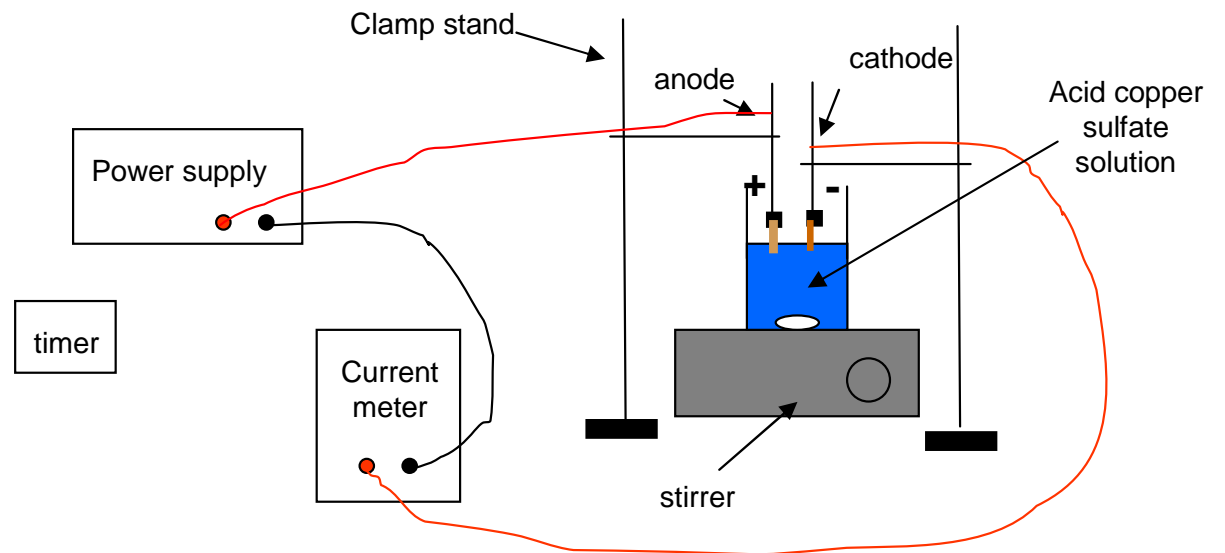
Copper sulphate ( $\text{CuSO}_4$ ) and sulphuric acid ( $\text{H}_2\text{SO}_4$ )

## Current density

Slightly rough to highly rough (Fractal)

## Masking

Mask and grow pillars in Cu on Cu



*Setup for the copper plating*